1. If α and β are roots of the equation $x^2+x+1=0$ then $\alpha^2+\beta^2$ is

   (a) -1 (b) $\frac{-1-i\sqrt{3}}{2}$ (c) $\frac{-1+i\sqrt{3}}{2}$ (d) 1

   Ans: (a)

   Sol: $\alpha+\beta=-1, \quad \alpha\beta=1$

   $\therefore \quad \alpha^2+\beta^2=-1$

2. The number of 4 digit numbers without repetition that can be formed using the digits 1, 2, 3, 4, 5, 6, 7 in which each number has two odd digits and two even digits is

   (a) 454 (b) 450 (c) 436 (d) 432

   Ans: (d)

   Sol: ${}^4C_2 \times {}^3C_2 \times 4! = 432$

3. The number of terms in the expansion of $\left(x^2+y^2\right)^{25}-\left(x^2-y^2\right)^{25}$ after simplification is

   (a) 50 (b) 26 (c) 13 (d) 0

   Ans: (c)

   Sol: No. of terms $=13$

4. The third term of a G.P. is 9. The product of its first five terms is

   (a) 3^{12} (b) 3^{10} (c) 3^9 (d) 3^5

   Ans: (b)

   Sol: Given, $ar^2=9$

   $\therefore \left(ar^2\right)^5=9^5=3^{10}$

5. A line cuts off equal intercepts on the co-ordinate axes. The angle made by this line with the positive direction of X-axis is

   (a) $135°$ (b) $120°$ (c) $90°$ (d) $45°$

   Ans: (a)

   Sol: $\theta=135°$

6. The order of the differential equation $y=C_1e^{C_3+x}+C_3e^{C_4+x}$ is

   (a) 4 (b) 3 (c) 2 (d) 1

   Ans: (c)

   Sol: $y=C_1e^{c_2}e^x+C_3e^{c_4}x$

   $\therefore$ order is 2

7. If $|\vec{a}| = 16. |\vec{b}| = 4$ then

$\sqrt{|\vec{a}\times\vec{b}|^2 + |\vec{a}\cdot\vec{b}|^2} =$

(a) 64 (b) 16 (c) 8 (d) 4

Ans: (a)

Sol: $\sqrt{|\vec{a}\times\vec{b}|^2 + |\vec{a}\cdot\vec{b}|^2} = |\vec{a}||\vec{b}| = 64$

8. If the angle between $\vec{a}$ and $\vec{b}$ is $\frac{2\pi}{3}$ and the projection of $\vec{a}$ in the direction of $\vec{b}$ is -2, then $|\vec{a}| =$

(a) 1 (b) 2 (c) 3 (d) 4

Ans: (d)

Sol: $\vec{a}\cdot\vec{b} = -2 \Rightarrow |\vec{a}|\cos\frac{2\pi}{3} = -2$

$\therefore |\vec{a}| = 4$

9. A unit vector perpendicular to the plane containing the vectors $\hat{i} + 2\hat{j} + \hat{k}$ and $-2\hat{i} + \hat{j} + 3\hat{k}$ is

(a) $\frac{-\hat{i} - \hat{j} - \hat{k}}{\sqrt{3}}$ (b) $\frac{-\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$ (c) $\frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$ (d) $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

Ans: (b)

Sol: By verification: Required Vector $= \frac{-\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$

10. $\left[\vec{a} + 2\vec{b} - \vec{c},\ \vec{a} - \vec{b},\ \vec{a} - \vec{b} - \vec{c}\right] =$

(a) $3\left[\vec{a}, \vec{b}, \vec{c}\right]$ (b) $2\left[\vec{a}, \vec{b}, \vec{c}\right]$ (c) $\left[\vec{a}, \vec{b}, \vec{c}\right]$ (d) 0

Ans: (d)

Sol: $\left[\vec{a} + 2\vec{b} - \vec{c} \quad \vec{a} - \vec{b} \quad \vec{a} - \vec{b} - \vec{c}\right] = \begin{vmatrix} 1 & 2 & -1 \\ 1 & -1 & 0 \\ 1 & -1 & -1 \end{vmatrix} \left[\vec{a} \quad \vec{b} \quad \vec{c}\right] = 0$

11. If $\sqrt[3]{y}\sqrt{x} = \sqrt[6]{(x+y)^5}$, then $\frac{dy}{dx} =$

(a) $\frac{y}{x}$ (b) $x - y$ (c) $x + y$ (d) $\frac{x}{y}$

Ans: (a)

Sol: Standard result: $\frac{dy}{dx} = \frac{y}{x}$

12. Rolle's theorem is not applicable in which one of the following cases?

(a) $f(x)=[x]$ in $[2.5,\ 2.7]$ (b) $f(x)=|x|$ in $[-2,\ 2]$

(c) $f(x)=x^2-x$ in $[0,\ 1]$ (d) $f(x)=x^2-4x+5$ in $[1,\ 3]$

Ans: (b)

Sol: By verification

$f(x)=|x|$ in $[-2,\ 2]$ as $|x|$ is not differentiable at $x=0$

13. The interval in which the function $f(x)=x^3-6x^2+9x+10$ is increasing in

(a) $(-\infty,\ -1]\cup[3,\ \infty)$ (b) $[1,\ 3]$ (c) $(-\infty,\ 1]\cup[3,\ \infty)$ (d) $(-\infty,\ 1)\cup(3,\ \infty)$

Ans: (c)

Sol: $f(x)=x^3-6x^2+9x+10$

$f'(x)>0 \Rightarrow 3x^2-12x+9>0$

$\Rightarrow x\in(-\infty,\ 1]\cup[3,\ \infty)$

14. The sides of an equilateral triangle are increasing at the rate of 4 cm/sec. the rate at which its area is increasing when the side is 14 cm

(a) $14\ \text{cm}^2/\text{sec}$ (b) $42\ \text{cm}^2/\text{sec}$ (c) $14\sqrt{3}\ \text{cm}^2/\text{sec}$ (d) $10\sqrt{3}\ \text{cm}^2/\text{sec}$

Ans: () **Grace Marks**

Sol: Options does not match $\left(28\sqrt{3}\ \text{cm}^2/\text{sec}\right)$

15. The value of $\sqrt{24.99}$ is

(a) 4.897 (b) 5.001 (c) 4.899 (d) 4.999

Ans: (d)

Sol: $\sqrt{24.99}=4.999$

16. If $|3x-5|\le 2$ then

(a) $-1\le x\le\frac{9}{3}$ (b) $1\le x\le\frac{9}{3}$ (c) $1\le x\le\frac{7}{3}$ (d) $-1\le x\le\frac{7}{3}$

Ans: (c)

Sol: $|3x-5|\le 2$

$-2\le 3x-5\le 2$

$\Rightarrow 1\le x\le\frac{7}{3}$

17. A random variable 'X' has the following probability distribution

X	1	2	3	4	5	6	7
$P(X)$	$k-1$	$3k$	k	$3k$	$3k^2$	k^2	k^2+k

Then the value of k is

(a) $\frac{1}{10}$ (b) $\frac{2}{7}$ (c) -2 (d) $\frac{1}{5}$

Ans: (d)

Sol: Sum of the probabilities $=1$

$\Rightarrow k=\frac{1}{5}$

18. If A and B are two events of a sample space S such that $P(A)=0.2, P(B)=0.6$ and $P(A|B)=0.5$ then $P(A'|B)=$

(a) $\frac{1}{3}$ (b) $\frac{1}{2}$ (c) $\frac{2}{3}$ (d) $\frac{3}{10}$

Ans: (b)

Sol: $P(A\cap B)=0.3$

$P(A'/B)=\frac{0.3}{0.6}=\frac{1}{2}$

19. If 'X' has a binomial distribution with parameters $n=6, p$ and $P(X=2)=12, P(X=3)=5$ then $P=$

(a) $\frac{5}{16}$ (b) $\frac{1}{2}$ (c) $\frac{16}{21}$ (d) $\frac{5}{12}$

Ans: () **Grace Marks**

Sol: Options does not match $\left(P=\frac{5}{21}\right)$

20. A man speaks truth 2 out of 3 times. He picks one of the natural numbers in the set $S=\{1, 2, 3, 4, 5, 6, 7\}$ and reports that it is even. The probability that it is actually even is

(a) $\frac{3}{5}$ (b) $\frac{1}{10}$ (c) $\frac{1}{5}$ (d) $\frac{2}{5}$

Ans: (a)

Sol: Required probability $=\dfrac{\frac{3}{7}\times\frac{2}{3}}{\frac{3}{7}\times\frac{2}{3}+\frac{4}{7}\times\frac{1}{3}}=\frac{3}{5}$

21. $\int_{-3}^{3} \cot^{-1} x dx =$

(a) 3 (b) 6π (c) 0 (d) 3π

Ans: (d)

Sol: $\int_{-3}^{3} \cot^{-1} x\, dx = \int_{-3}^{3} \left(\frac{\pi}{2} - \tan^{-1} x\right) dx$

$= \frac{\pi}{2}(3+3) - 0 = 3\pi$

22. $\int \frac{1}{\sqrt{x} + x\sqrt{x}} dx =$

(a) $2\tan^{-1}\sqrt{x} + C$ (b) $\tan^{-1}\sqrt{x} + C$ (c) $\frac{1}{2}\tan^{-1}\sqrt{x} + C$ (d) $2\log\left(\sqrt{x}+1\right) + C$

Ans: (a)

Sol: $\int \frac{1}{\sqrt{x}(1+x)}\, dx = 2\tan^{-1}\sqrt{x} + C$

23. $\int \frac{2x-1}{(x-1)(x+2)(x-3)} dx = A\log|x-1| + B\log|x+2| + C\log|x-3| + K$, then $A,\ B,\ C$ are respectively

(a) $\frac{-1}{6}, \frac{-1}{3}, \frac{1}{2}$ (b) $\frac{1}{6}, \frac{-1}{3}, \frac{1}{3}$ (c) $\frac{1}{6}, \frac{1}{3}, \frac{1}{5}$ (d) $\frac{-1}{6}, \frac{1}{3}, \frac{-1}{2}$

Ans: (a)

Sol: By verification, $A = \frac{-1}{6},\ B = \frac{-1}{3},\ C = \frac{1}{2}$

24. $\int_{0}^{2} \left[x^2\right] dx =$

(a) $-5-\sqrt{2}-\sqrt{3}$ (b) $5-\sqrt{2}+\sqrt{3}$ (c) $5+\sqrt{2}-\sqrt{3}$ (d) $5-\sqrt{2}-\sqrt{3}$

Ans: (d)

Sol: $\int_{0}^{1} 0\, dx + \int_{1}^{\sqrt{2}} 1\, dx + \int_{\sqrt{2}}^{\sqrt{3}} 2\, dx + \int_{\sqrt{3}}^{2} 3\, dx$

$= \sqrt{2} - 1 + 2\sqrt{3} - 2\sqrt{2} + 6 - 3\sqrt{3}$

$= 5 - \sqrt{2} - \sqrt{3}$

25. $\int_0^1 \sqrt{\frac{1+x}{1-x}}dx =$

(a) $\frac{1}{2}$ (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{2}+1$ (d) $\frac{\pi}{2}-1$

Ans: (c)

Sol: $\int_0^1 \frac{1+x}{\sqrt{1-x^2}}\, dx = \left[\sin^{-1} x - \sqrt{1-x^2}\right]_0^1$

$= \frac{\pi}{2}+1$

26. $f:\mathbb{R} \to \mathbb{R}$ and $g:[0,\infty) \to \mathbb{R}$ is defined by $f(x)=x^2$ and $g(x)=\sqrt{x}$. Which one of the following is not true?

(a) $g \circ f(-2)=2$ (b) $f \circ g(2)=2$ (c) $f \circ g(-4)=4$ (d) $g \circ f(4)=4$

Ans: (c)

Sol: By verification: $fog(-4) \neq 4$

27. $A=\{x|x \in \mathbb{N}\, x \le 5\}, B=\{x|x \in \mathbb{N}, x^2-5x+6=0\}$, then the number of onto functions from A to B is

(a) 32 (b) 30 (c) 23 (d) 2

Ans: (b)

Sol: $A=\{1, 2, 3, 4, 5\}$, $B=\{2, 3\}$

No. of Onto functions $=2^5-2=30$

28. On the set of positive rationals, a binary operation * is defined by

$a*b=\frac{2ab}{5}$.

If $2*x=3^{-1}$ then $x=$

(a) $\frac{125}{48}$ (b) $\frac{2}{5}$ (c) $\frac{5}{12}$ (d) $\frac{1}{6}$

Ans: (a)

Sol: $e=\frac{5}{2}, 3^{-1}=\frac{25}{12}$ $\quad \therefore\ 2*x=3^{-1}$

$\Rightarrow x=\frac{125}{48}$

29. $\cos\left[2\sin^{-1}\frac{3}{4}+\cos^{-1}\frac{3}{4}\right]=$

(a) does not exist (b) $\frac{3}{5}$ (c) $\frac{3}{4}$ (d) $\frac{-3}{4}$

Ans: (d)

Sol: $\cos\left(\frac{\pi}{2}+\sin^{-1}\frac{3}{4}\right)=\frac{-3}{4}$

30. If $a+\frac{\pi}{2}<2\tan^{-1}x+3\cot^{-1}x<b$ then 'a' and 'b' are respectively.

(a) $\frac{-\pi}{2}$ and $\frac{\pi}{2}$ (b) 0 and 2π (c) $\frac{\pi}{2}$ and 2π (d) 0 and π

Ans: (c)

Sol: $a+\frac{\pi}{2}<\pi+\cot^{-1}x<b$

$a-\frac{\pi}{2}<\cot^{-1}x<-\pi+b$ but $0<\cot^{-1}x<\pi$

$\therefore\ a=\frac{\pi}{2},\ b=2\pi$

31. If U is the universal set with 100 elements; A and B are two sets such that $n(A)=50$, $n(B)=60$, $n(A\cap B)=20$ then $n(A'\cap B')=$

(a) 10 (b) 90 (c) 20 (d) 40

Ans: (a)

Sol: $n(A'\cap B')=n(U)-\left(n(A)+n(B)-n(A\cap B)\right)=10$

32. The domain of the function $f:\mathbb{R}\to\mathbb{R}$ defined by $f(x)=\sqrt{x^2-7x+12}$ is

(a) $(3,4)$ (b) $(-\infty,3]\cap[4,\infty)$ (c) $(-\infty,3]\cup(4,\infty)$ (d) $(-\infty,3]\cup[4,\infty)$

Ans: (d)

Sol: $x^2-7x+12\geq 0 \Rightarrow x\in(-\infty,3]\cup[4,\infty)$

33. If $\cos x=|\sin x|$ then, the general solution is

(a) $x=(2n+1)\pi\pm\frac{\pi}{4},n\in\mathbb{Z}$ (b) $x=n\pi+(-1)^n\frac{\pi}{4},n\in\mathbb{Z}$

(c) $x=2n\pi\pm\frac{\pi}{4},n\in\mathbb{Z}$ (d) $x=n\pi\pm\frac{\pi}{4},n\in\mathbb{Z}$

Ans: (d)

Sol: $\cos x=|\sin x|$

$\Rightarrow \tan x=\pm 1 \quad \therefore\ x=n\pi\pm\frac{\pi}{4},\ n\in\mathbb{Z}$

34. $\sqrt{3}\operatorname{cosec}20^\circ - \sec 20^\circ =$

(a) 1 (b) 4 (c) 3 (d) 2

Ans: (b)

Sol: $\sqrt{3}\operatorname{cosec}20^\circ - \sec 20^\circ = \dfrac{2\sin 40^\circ}{\dfrac{\sin 40^\circ}{2}} = 4$

35. If $P(n): 2^n < n!$ then the smallest positive integer for which $P(n)$ is true, is

(a) 5 (b) 4 (c) 3 (d) 2

Ans: (b)

Sol: By verification $n = 4$

36. Foot of the perpendicular drawn from the point $(1,3,4)$ to the plane $2x - y + z + 3 = 0$ is

(a) $(-3,5,2)$ (b) $(1,2,-3)$ (c) $(0,-4,-7)$ (d) $(-1,4,3)$

Ans: (d)

Sol: $\dfrac{h-x_1}{a} = \dfrac{k-y_1}{b} = \dfrac{l-z_1}{c} = -\dfrac{(ax_1+by_1+cz_1+d)}{a^2+b^2+c^2}$

Foot of perpendicular $(h,\ k,\ l) = (-1,\ 4,\ 3)$

37. Acute angle between the line $\dfrac{x-5}{2} = \dfrac{y+1}{-1} = \dfrac{z+4}{1}$ and the plane $3x - 4y - z + 5 = 0$ is

(a) $\sin^{-1}\left(\dfrac{5}{2\sqrt{13}}\right)$ (b) $\cos^{-1}\left(\dfrac{5}{2\sqrt{13}}\right)$ (c) $\sin^{-1}\left(\dfrac{9}{\sqrt{364}}\right)$ (d) $\cos^{-1}\left(\dfrac{9}{\sqrt{364}}\right)$

Ans: (b)

Sol: $\sin\theta = \dfrac{9}{2\sqrt{39}} \Rightarrow \cos\theta = \dfrac{5}{2\sqrt{13}} \quad \therefore \quad \theta = \cos^{-1}\left(\dfrac{5}{2\sqrt{13}}\right)$

38. The distance of the point $(1,2,1)$ from the line $\dfrac{x-1}{2} = \dfrac{y-2}{1} = \dfrac{z-3}{2}$ is

(a) $\dfrac{20}{3}$ (b) $\dfrac{\sqrt{5}}{3}$ (c) $\dfrac{2\sqrt{5}}{3}$ (d) $\dfrac{2\sqrt{3}}{5}$

Ans: (d)

Sol: Hint: $r = \dfrac{-4}{9}$, Foot of perpendicular $= \left(\dfrac{1}{9}, \dfrac{14}{9}, \dfrac{19}{9}\right)$

By distance formula, Distance $= \dfrac{2\sqrt{5}}{3}$

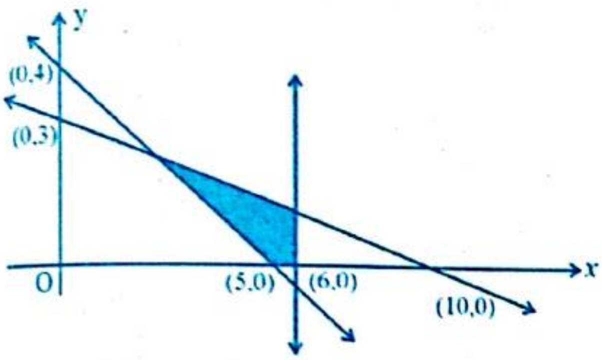
39. XY-plane divides the line joining the points $A(2,3,-5)$ and $B(-1,-2,-3)$ in the ratio

(a) 5 : 3 externally (b) 5 : 3 internally (c) 3 : 2 externally (d) 2 : 1 internally

Ans: (b)

Sol: $5:3$ externally. Hint: $-z_1 : z_2$

40. The shaded region in the figure is the solution set of the inequations



(a) $4x+5y \le 20,\ 3x+10y \le 30,\ x \ge 6,\ x,\ y \ge 0$

(b) $4x+5y \le 20,\ 3x+10y \le 30,\ x \le 6,\ x,\ y \ge 0$

(c) $4x+5y \ge 20,\ 3x+10y \le 30,\ x \ge 6,\ x,\ y \ge 0$

(d) $4x+5y \ge 20,\ 3x+10y \le 30,\ x \le 6,\ x,\ y \ge 0$

Ans: (d)

Sol: Verification: $4x+5y \ge 20,\ 3x+10y \le 30,\ x \le 6,\ x,\ y \ge 0$

41. The inverse of the matrix $\begin{bmatrix} 2 & 5 & 0 \\ 0 & 1 & 1 \\ -1 & 0 & 3 \end{bmatrix}$ is

(a) $\begin{bmatrix} 3 & -15 & 5 \\ -1 & 6 & -2 \\ 1 & -5 & -2 \end{bmatrix}$ (b) $\begin{bmatrix} 3 & -15 & 5 \\ -1 & 6 & -2 \\ 1 & -5 & 2 \end{bmatrix}$ (c) $\begin{bmatrix} 3 & -5 & 5 \\ -1 & -6 & -2 \\ 1 & -5 & 2 \end{bmatrix}$ (d) $\begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$

Ans: (b)

Sol: verification: Inverse is $\begin{bmatrix} 3 & -15 & 5 \\ -1 & 6 & -2 \\ 1 & -5 & 2 \end{bmatrix}$

42. If P and Q are symmetric matrices of the same order then $PQ-QP$ is

(a) skew symmetric matrix (b) zero matrix

(c) symmetric matrix (d) identity matrix

Ans: (a)

Sol: $PQ-QP$ is skew symmetric

43. If $3A+4B'=\begin{bmatrix}7 & -10 & 17\\0 & 6 & 31\end{bmatrix}$ and $2B-3A'=\begin{bmatrix}-1 & 18\\4 & 0\\-5 & -7\end{bmatrix}$ then $B=$

(a) $\begin{bmatrix}1 & 3\\-1 & 1\\2 & -4\end{bmatrix}$ (b) $\begin{bmatrix}-1 & -18\\4 & -16\\-5 & -7\end{bmatrix}$ (c) $\begin{bmatrix}1 & -3\\-1 & 1\\2 & 4\end{bmatrix}$ (d) $\begin{bmatrix}1 & 3\\-1 & 1\\2 & 4\end{bmatrix}$

Ans: (d)

Sol: $3A+4B'=X$

$-3A+2B'=Y \quad \therefore \quad B=\begin{bmatrix}1 & 3\\-1 & 1\\2 & 4\end{bmatrix}$

44. If $A=\begin{bmatrix}1 & 3\\4 & 2\end{bmatrix}$, $B=\begin{bmatrix}2 & -1\\1 & 2\end{bmatrix}$, then $|ABB'|=$

(a) 250 (b) 100 (c) -250 (d) 50

Ans: (c)

Sol: $|ABB'|=|A||B||B'|=-250$

45. If the value of a third order determinant is 16, then the value of the determinant formed by replacing each of its elements by its cofactor is

(a) 16 (b) 256 (c) 48 (d) 96

Ans: (b)

Sol: $|A|^2=256$

46. The eccentricity of the ellipse $9x^2+25y^2=225$ is

(a) $\frac{9}{16}$ (b) $\frac{3}{4}$ (c) $\frac{3}{5}$ (d) $\frac{4}{5}$

Ans: (d)

Sol: $e=\frac{4}{5}$

47. $\sum_{r=1}^{n}(2r-1)=x$ then $\lim_{n\to\infty}\left[\frac{1^3}{x^2}+\frac{2^3}{x^2}+\frac{3^3}{x^2}+\cdots\cdots+\frac{n^3}{x^2}\right]=$

(a) 4 (b) 1 (c) $\frac{1}{4}$ (d) $\frac{1}{2}$

Ans: (c)

Sol: Given, $x=n^2$

$\lim_{n\to\infty}\frac{\sum n^3}{n^4}=\frac{1}{4}$

48. The negation of the statement "All continuous functions are differentiable."

(a) All differentiable functions are continuous

(b) Some continuous functions are not differentiable

(c) Some continuous functions are differentiable

(d) All continuous functions are differentiable

Ans: (b)

Sol: Some continuous functions are not differentiable

49. Mean and standard deviation of 100 items are 50 and 4 respectively. The sum of all squares of the items is

(a) 261600 (b) 266000 (c) 256100 (d) 251600

Ans: (d)

Sol: $\sum x_i^2 = 251600$

50. Two letters are chosen from the letters of the word 'EQUATIONS'. The probability that one is vowel and the other is consonant is

(a) $\frac{5}{9}$ (b) $\frac{3}{9}$ (c) $\frac{4}{9}$ (d) $\frac{8}{9}$

Ans: (a)

Sol: $\frac{5\times 4}{{}^9C_2} = \frac{5}{9}$

51. $\int x^3 \sin 3x \, dx =$

(a) $-\frac{x^3 \cos 3x}{3} + \frac{x^2 \sin 3x}{3} - \frac{2x\cos 3x}{9} - \frac{2\sin 3x}{27} + C$

(b) $-\frac{x^3 \cos 3x}{9} + \frac{x^2 \sin 3x}{3} + \frac{2x\cos 3x}{9} - \frac{2\sin 3x}{27} + C$

(c) $\frac{x^3 \cos^3}{3} + \frac{x^2 \sin 3x}{3} - \frac{2x\cos 3x}{9} - \frac{2\sin 3x}{27} + C$

(d) $-\frac{x^3 \cos 3x}{3} - \frac{x^2 \sin 3x}{3} + \frac{2x\cos 3x}{9} - \frac{2\sin 3x}{27} + C$

Ans: (a)

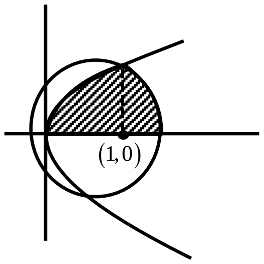
Sol: $\int x^3 \sin 3x \, dx = \frac{-x^3}{3}\cos 3x + \frac{x^2 \sin 3x}{3} - \frac{2x\cos 3x}{9} - \frac{2\sin 3x}{27} + C$

52. The area of the region above X- axis included between the parabola $y^2 = x$ and the circle $x^2 + y^2 = 2x$ in square units is

(a) $\frac{\pi}{4} - \frac{2}{3}$ (b) $\frac{2}{3} - \frac{\pi}{4}$ (c) $\frac{3}{2} - \frac{\pi}{4}$ (d) $\frac{\pi}{4} - \frac{3}{2}$

Ans: () **Grace Marks**

Sol: Required area $= \frac{\pi}{4} + \frac{2}{3}$



Option does not match

53. The area of the region bounded by Y-axis, $y = \cos x$ and $y = \sin x; 0 \le x \le \frac{\pi}{2}$ is

(a) $2\sqrt{2}$ $Sq.$ units (b) $\sqrt{2} + 1$ $Sq.$ units (c) $\sqrt{2}$ $Sq.$ units (d) $\sqrt{2} - 1$ $Sq.$ units

Ans: (d)

Sol: Required Area $= \sqrt{2} - 1$ sq. units

54. The integrating factor of the differential equation $\left(2x + 3y^2\right)dy = y\,dx \left(y > 0\right)$ is

(a) $\frac{1}{y^2}$ (b) $\frac{1}{x}$ (c) $-\frac{1}{y^2}$ (d) $e^{\frac{1}{y}}$

Ans: (a)

Sol: $\frac{dx}{dy} - \frac{2x}{y} = 3y$

$\therefore$ I.F $= e^{-2\log y} = \frac{1}{y^2}$

55. The equation of the curve passing through the point $(1, 1)$ such that the slope of the tangent at any point (x, y) is equal to the product of its co-ordinates is

(a) $2\log x = y^2 + 1$ (b) $2\log y = x^2 - 1$ (c) $2\log y = x^2 + 1$ (d) $2\log x = y^2 - 1$

Ans: (b)

Sol: $\frac{dy}{dx} = xy$

$\Rightarrow \log y = \frac{x^2}{2} + C,\ C = \frac{-1}{2}$

$\therefore\ 2\log y = x^2 - 1$

56. The constant term in the expansion of $\begin{vmatrix} 3x+1 & 2x-1 & x+2 \\ 5x-1 & 3x+2 & x+1 \\ 7x-2 & 3x+1 & 4x-1 \end{vmatrix}$ is

(a) 6 (b) -10 (c) 2 (d) 0

Ans: (a)

Sol: $\begin{vmatrix} 1 & -1 & 2 \\ -1 & 2 & 1 \\ -2 & 1 & 1 \end{vmatrix} = 6$ (By putting $x = 0$)

57. If $[x]$ represents the greatest integer function and $f(x) = x - [x] - \cos x$ then $f'\left(\frac{\pi}{2}\right) =$

(a) does not exist (b) 2 (c) 1 (d) 0

Ans: (b)

Sol: $f'\left(\frac{\pi}{2}\right) = 1 + \sin\frac{\pi}{2} = 2$

58. If $f(x) = \begin{cases} \frac{\sin 3x}{e^{2x}-1} & ; \ x \neq 0 \\ k-2 & ; \ x = 0 \end{cases}$ is continuous at $x = 0$, then $k =$

(a) $\frac{2}{3}$ (b) $\frac{1}{2}$ (c) $\frac{9}{5}$ (d) $\frac{3}{2}$

Ans: () **(Grace Marks)**

Sol: Options does not match $\left(k = \frac{7}{2}\right)$

59. If $f(x) = \sin^{-1}\left[\frac{2^{x+1}}{1+4^x}\right]$, then $f'(0) =$

(a) $\frac{4\log 2}{5}$ (b) $\frac{2\log 2}{5}$ (c) $\log 2$ (d) $2\log 2$

Ans: (c)

Sol: $f(x) = \sin^{-1}\left(\frac{2 \cdot 2^x}{1+\left(2^x\right)^2}\right) = 2\tan^{-1} 2^x \ \therefore\ f'(0) = \log 2$

60. If $x = a\sec^2\theta,\ y = a\tan^2\theta$ then $\frac{d^2y}{dx^2} =$

(a) 4 (b) 0 (c) 1 (d) $2a$

Ans: (b)

Sol: $\frac{dy}{dx} = 1 \ \therefore\ \frac{d^2y}{dx^2} = 0$

Key Answers:

1. a	2. d	3. c	4. b	5. a	6. c	7. a	8. d	9. b	10. d
11. a	12. b	13. c	14.	15. d	16. c	17. d	18. b	19.	20. a
21. d	22. a	23. a	24. d	25. c	26. c	27. b	28. a	29. d	30. c
31. a	32. d	33. d	34. b	35. b	36. d	37. b	38. d	39. b	40. d
41. b	42. a	43. d	44. c	45. b	46. d	47. c	48. b	49. d	50. a
51. a	52.	53. d	54. a	55. b	56. a	57. b	58.	59. c	60. b

Q14: Grace

Q19: Grace

Q52: Grace

Q58: Grace